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Towards, Competitive, Reliable, Safe and Sustainable Concentrated Solar Power (CSP) Plants

Midterm meeting REA, 18-19 April 2024

DC 9: Coupled optimization of solar field and receiver/cavity
geometry and thermal/hydraulic design

Tom Todtenhaupt



- 1 Introduction
- 2 Receiver Optimization
- 3 Reduced Order Model
- 4 Future Work

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Introduction

Education:

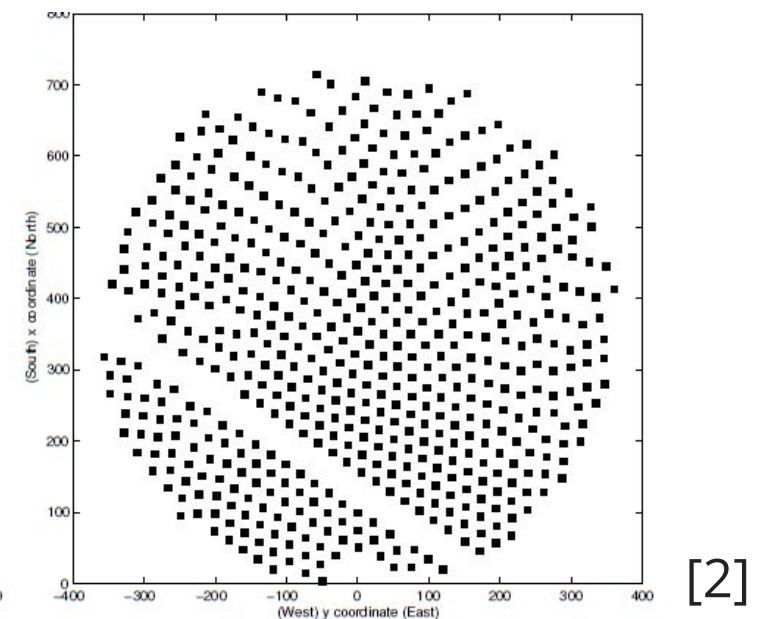
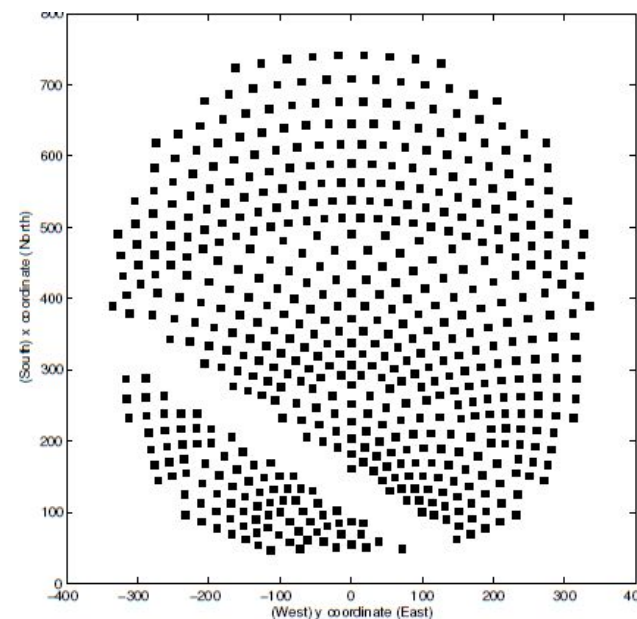
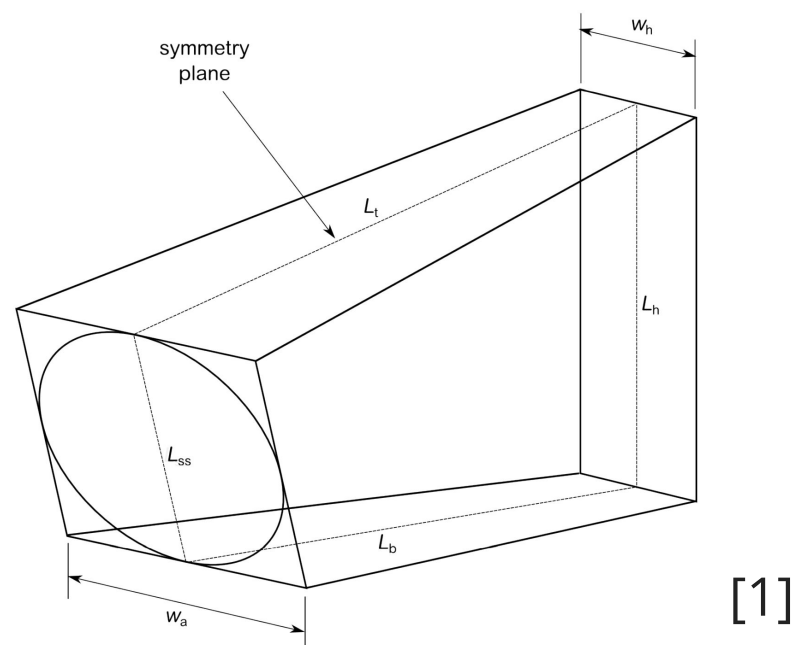
- Bachelor Mechanical Engineering, Clausthal University of Technology
- Master Mechanical Engineering, Clausthal University of Technology

Experience:

- Research assistant, Institute of Tribology and Energy Conversion Machinery, Clausthal-Zellerfeld
- Intern Audi Sport, Neuburg a.d. Donau
- PhD fellow TOPCSP, Sevilla

Introduction

- Central receiver/cavity geometry optimization
- Solar field optimization
- So far, these optimizations were done independently
- Goal: coupling these optimizations



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Receiver Optimization

Design parameters: $\chi = (L_1 \ L_2 \ L_4 \ \theta_1 \ \theta_2 \ w_1 \ w_2)$

Objective function: $Q_{ls} = Q_{conv} + Q_{rad} + Q_{opt}$

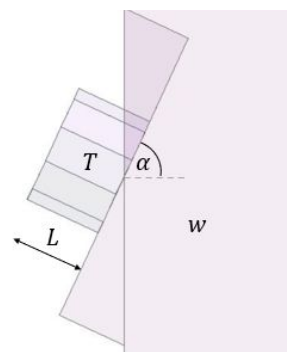
$$Q_{conv} = h \cdot A \cdot \Delta T \quad ; \quad h = \frac{Nu \cdot k}{L}$$

$$Nu = 0,122 \cdot Ra^{0,31} \cdot \left(\frac{T_w}{T_a} \right)^{0,066} \cdot (1 + \cos(\theta))^{0,38}$$

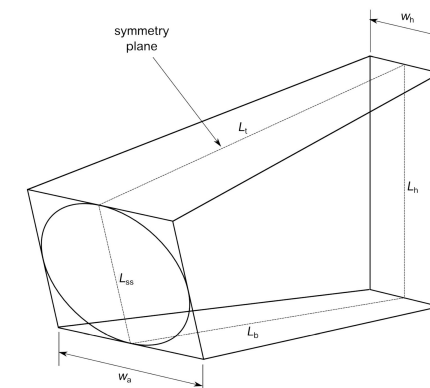
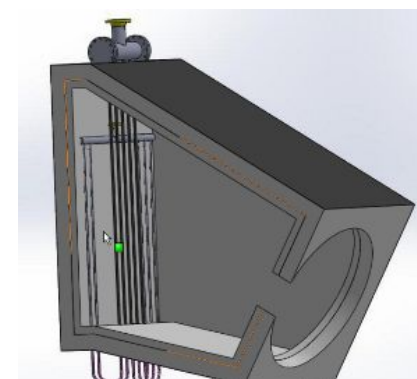
Optimization Problem:

$$\begin{aligned} & \text{minimize} \quad Q_{ls} = Q_{ls}(\chi, T_w, p) \\ & \text{subject to} \quad \chi_{lb} \leq \chi \leq \chi_{ub} \quad ; \quad g(\chi) \leq G \quad ; \quad h(\chi) = H \end{aligned}$$

Replace Nusselt-number-correlation with coupled Reduced-Order-Models for receiver design optimization



[3]



[1]

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Reduced Order Model

- Proper Orthogonal Decomposition / Singular Value Decomposition (SVD)

$$x_i \in \mathbb{R}^n \quad n \gg m$$

$$X = \begin{bmatrix} | & | & & | \\ x_1 & x_2 & \dots & x_m \\ | & | & & | \end{bmatrix} = U \Sigma V^T = \begin{bmatrix} | & | & & | \\ u_1 & u_2 & \dots & u_n \\ | & | & & | \end{bmatrix} \begin{bmatrix} \sigma_1 & & & \\ & \sigma_2 & & \\ & & \ddots & \\ & & & \sigma_m \\ 0 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} - & v_1^T & - \\ - & v_2^T & - \\ & \vdots & \\ - & v_m^T & - \end{bmatrix}$$

$$= \sigma_1 u_1 v_1^T + \sigma_2 u_2 v_2^T + \dots + \sigma_m u_m v_m^T + 0 \quad [4]$$

Reduced Order Model

- Proper Orthogonal Decomposition / Singular Value Decomposition (SVD)

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$$X = \begin{bmatrix} | & | & & | \\ x_1 & x_2 & \dots & x_m \\ | & | & & | \end{bmatrix} = U \Sigma V^T = \begin{bmatrix} | & | & & | \\ u_1 & u_2 & \dots & u_n \\ | & | & & | \end{bmatrix} \begin{bmatrix} \sigma_1 & & & \\ & \sigma_2 & & \\ & & \ddots & \\ & & & \sigma_m \\ 0 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} - & v_1^T & - \\ - & v_2^T & - \\ - & \vdots & - \\ - & v_m^T & - \end{bmatrix}$$

$$\sigma_1 u_1 v_1^T + \sigma_2 u_2 v_2^T + \dots + \cancel{\sigma_m u_m v_m^T} + 0 = \tilde{U} \tilde{\Sigma} \tilde{V}^T \quad [4]$$

Truncation at
rank r

Reduced Order Model



(a) Original image



(b) SVD Approximation of rank 5



(c) SVD Approximation of rank 150



(d) SVD Approximation of rank 500

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Reduced Order Model

SVD:

$$\begin{array}{c} \boxed{\tilde{X}} \\ n \times m \end{array} = \begin{array}{c} \boxed{\tilde{U}} \\ n \times r \end{array} \begin{array}{c} \boxed{\tilde{\Sigma}} \\ r \times r \end{array} \begin{array}{c} \boxed{\tilde{V}^T} \\ m \times r \end{array}$$

Higher-order SVD:

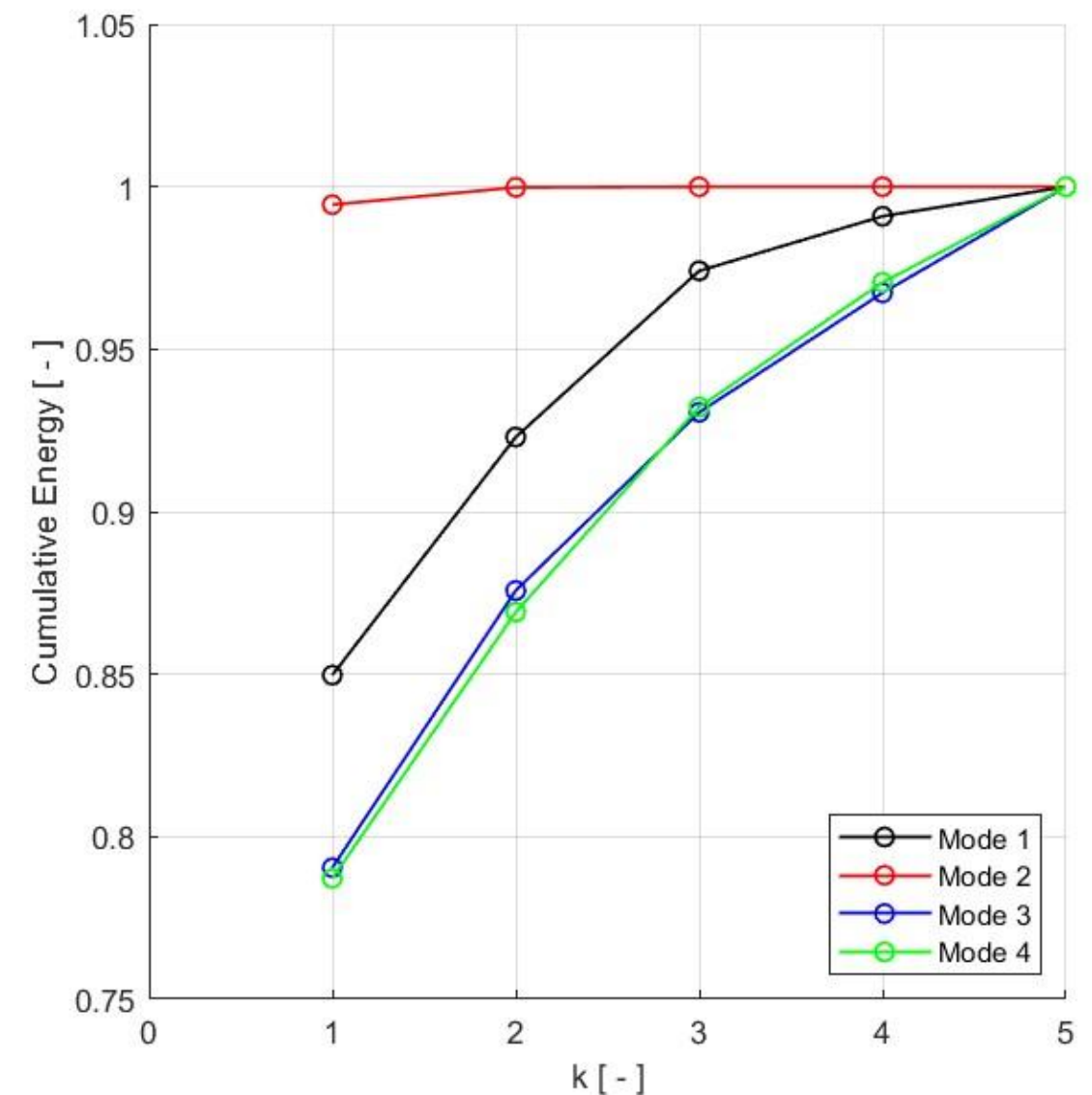
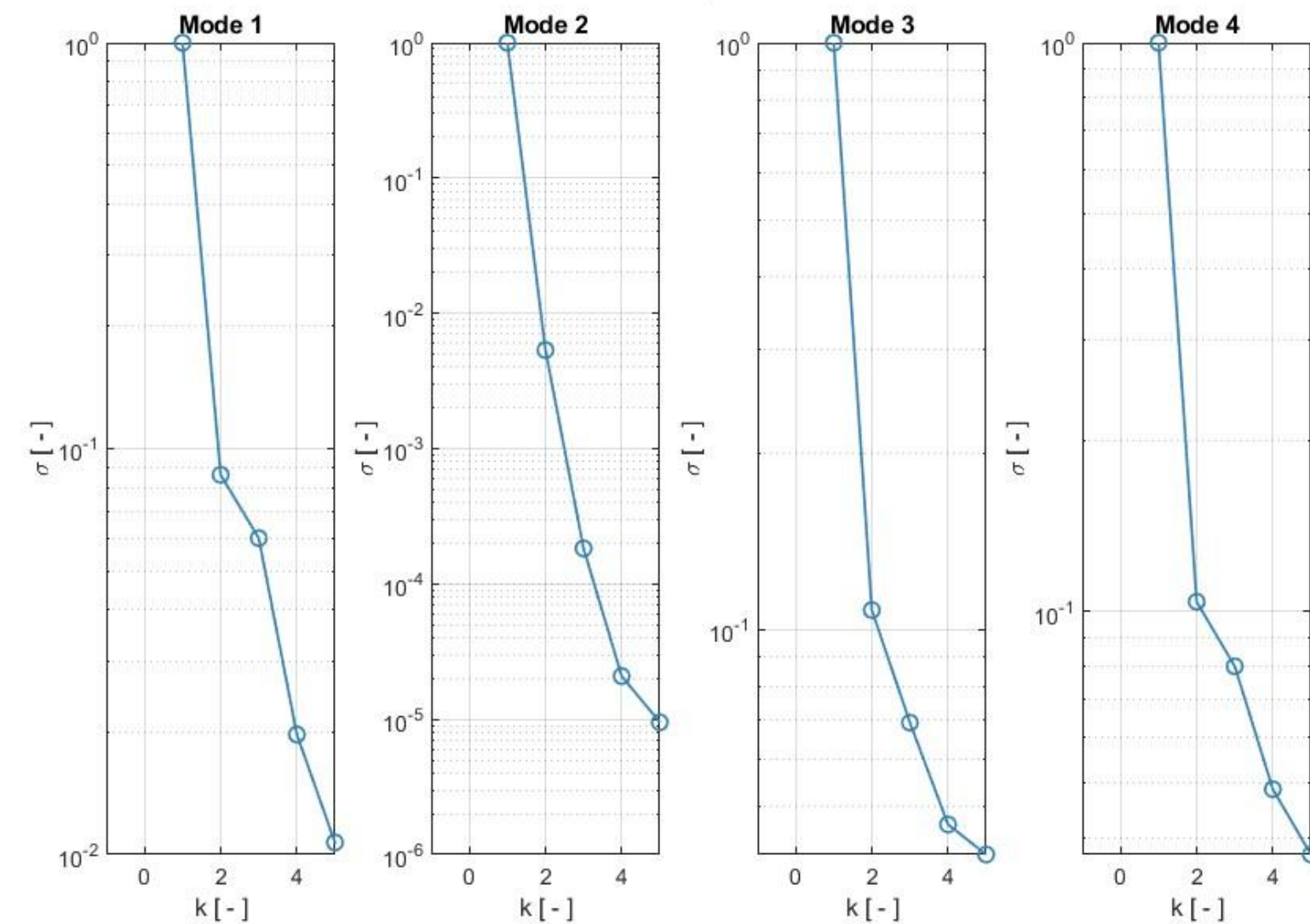
$$\begin{array}{c} \boxed{\tilde{X}} \\ n \times m \times p \end{array} = \begin{array}{c} \boxed{\tilde{U}} \\ n \times r_1 \end{array} \begin{array}{c} \boxed{\tilde{\Sigma}} \\ r_1 \times r_2 \times r_3 \end{array} \begin{array}{c} \boxed{\tilde{V}} \\ m \times r_2 \end{array} \begin{array}{c} \boxed{\tilde{W}} \\ p \times r_3 \end{array}$$

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Reduced Order Model

- Uncoupled Reduced-Order-Model of Solugas-type cavity receiver

Normalized singular values



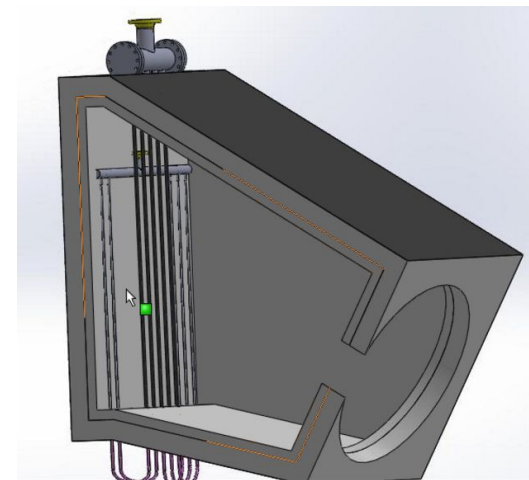
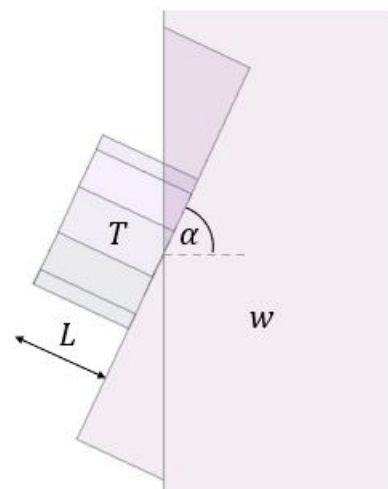
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Future work

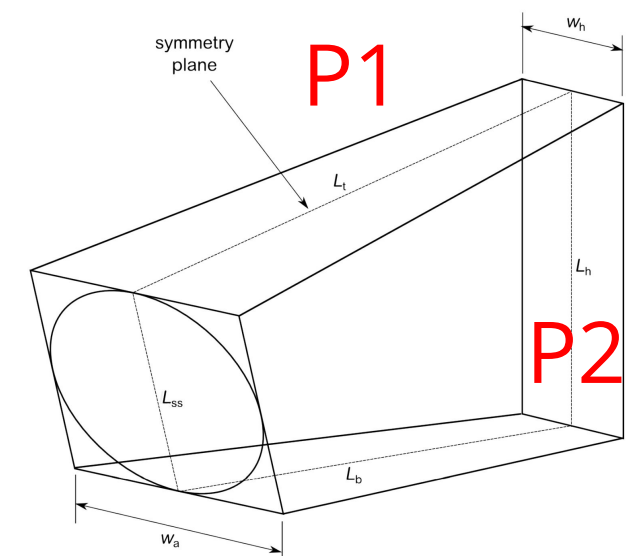
- Using raytracing results as an import for both Solugas and Cersol ROM's (coupling)
- Consider P2: heat transfer to fluid
- Building a database for machine learning



Solugas receiver [3]



Cersol receiver [1]





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Thank you for your attention!



References

- [1] Virtualmechanics S.L., TRANSFER (2022), p.31 fig. 19, *Cersol cavity receiver*
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- [3] Virtualmechanics S.L., TRANSFER (2022), p.52 fig. 44, *Photography of Solugas cavity receiver*
- [4] S. Brunton, N. Kutz, Data Driven Science & Engineering (2017), p.5, *Singular Value Decomposition, Overview*
- [5] C. Nuñez Fernández, Desarrollo y análisis de un modelo de orden reducido POD con viscosidad artificial (2022), p.25 fig. 3.1, *Approximation of the original images with lower rank*
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